Exercise 35. (a) For the following permutations $w$, draw $T(w)$ and $T^{\prime}(w)$. Verify that $T(w)$ and $T^{\prime}(w)$ are increasing.
(i) $w=68412537$
(ii) $w=12345$
(iii) $w=54321$
(b) Let


If $T=T(w)$, what is $w$ ? Verify that the double rises, double descents, valleys, and peaks of $w$ correspond to the correct behavior of successors.
(c) Let


If $T=T^{\prime}(w)$, what is $w$ ? Verify the following for $T^{\prime}(w)$.
(i) The successors of 0 are just the left-to-right minima of $w$.
(ii) The leaves are $D(w) \cup\{n\}$.
(d) Briefly justify each of (a)-(c) in Proposition 1.5.3 of EC1.
(e) Briefly justify each of (a)-(c) in Proposition 1.5.5 of EC1.

