## MATH 113: DISCRETE STRUCTURES HOMEWORK FOR FRIDAY WEEK 12

Problem 1. Use Sunzi's Theorem to efficiently compute the congruence class of $17^{2}$ modulo 35 . (What is the value to $\overline{17}^{2} \in \mathbb{Z} / 5 \mathbb{Z}$ ? and in $\mathbb{Z} / 7 \mathbb{Z}$ ? Use Sunzi's Theorem to push these results back into $\mathbb{Z} / 35 \mathbb{Z}$.)
Problem 2. Find all solutions to the system of congruences

$$
\begin{array}{ll}
x \equiv 1 & (\bmod 6) \\
x \equiv 4 & (\bmod 15) .
\end{array}
$$

Prove all your assertions along the way. (Careful! The moduli 6 and 15 are not relatively prime, so you can't appeal to Sunzi's Theorem.)

