## MATH 113: DISCRETE STRUCTURES HOMEWORK FOR FRIDAY WEEK 12

*Problem* 1. Use Sunzi's Theorem to efficiently compute the congruence class of  $17^2$  modulo 35. (What is the value to  $\overline{17}^2 \in \mathbb{Z}/5\mathbb{Z}$ ? and in  $\mathbb{Z}/7\mathbb{Z}$ ? Use Sunzi's Theorem to push these results back into  $\mathbb{Z}/35\mathbb{Z}$ .)

*Problem* 2. Find all solutions to the system of congruences

$$\begin{array}{ll} x\equiv 1 \pmod{6} \\ x\equiv 4 \pmod{15}. \end{array}$$

Prove all your assertions along the way. (*Careful!* The moduli 6 and 15 are not relatively prime, so you can't appeal to Sunzi's Theorem.)