

# Math 441

## Homework 4

Due Monday, April 6

1. Textbook problem 11.4
2. Textbook problem 11.6
3. Say you are encrypting a message using plain RSA encryption (construction 11.26 in the book). Say that the key generation algorithm picks  $p$  and  $q$  to be 503 and 521 and that we are using  $e = 3$ . What is the public key? What is the private key? Say  $m = 1435$ . What will the encryption of  $m$  be? Say you saw a ciphertext of  $c = 130$ . What would the decryption of that ciphertext be?
4. Alice has a complaint about RSA encryption. In particular, the message space is the group  $\mathbb{Z}_N^*$ , since numbers not in that group can't be multiplied (or exponentiated) in an invertible way mod  $N$ . But without knowing the factors of  $N$ , how can the sender check to make sure the message is in that group? Is Alice's complaint a serious concern? Why or why not?