Math 387

Homework 3

Due Friday, September 25

Practice exercises from the book

 $2.1,\ 2.4,\ 2.5,\ 2.6,\ 2.9,\ 2.10,\ 2.15$

Problems

- 1. For each of the following languages, give a CFG that generates the language. In all cases $\Sigma = \{0, 1\}$.
 - (a) $L = \{w \mid w \text{ contains at least three 1s}\}.$
 - (b) $L = \{w \mid w \text{ has odd length and its middle symbol is } 0\}.$
 - (c) $L = \{0^m 1^n \mid m \neq n\}.$
 - (d) $L = \{w \mid w \text{ has exactly twice as many 0s as 1s}\}.$
- 2. Draw the state diagram of a PDA that accepts each of the following languages. In all cases $\Sigma = \{0, 1\}$.
 - (a) $L = \{0^m 1^n \mid m \neq n\}.$
 - (b) $L = \{w \mid w \text{ contains more 0s than 1s}\}.$

Bonus problems

1. Let G be the following CFG:

$$S \to \mathbf{a}S\mathbf{b} \mid \mathbf{b}Y \mid Y\mathbf{a}$$
$$Y \to \mathbf{b}Y \mid \mathbf{a}Y \mid \epsilon$$

Give a simple English description of the language of G. Use this description to give a CFG that recognizes the complement of that language.

- 2. $L = \{xy \mid |x| = |y| \text{ and } x \neq y\}.$
 - (a) Give a CFG that generates the language L.
 - (b) Give a PDA that accepts the language L.