## MATH 412: TOPICS IN ALGEBRA HOMEWORK DUE FRIDAY WEEK 10

*Problem* 1. For  $\lambda \in k^{\times}$ , determine  $G(2\langle \lambda \rangle)$  and  $G(4\langle \lambda \rangle)$ .

*Problem* 2. For any Pfister form f, show that  $\langle\!\langle \lambda \rangle\!\rangle \otimes f \cong \langle\!\langle \mu \rangle\!\rangle \otimes f$  if and only if  $\lambda \mu \in D(f)$ .

*Problem* 3 (Bonus). Show that if n is a power of 2, then

$$D(n\langle 1\rangle) \cdot D((n+1)\langle 1\rangle) = D(2n\langle 1\rangle).$$