MATH 113: DISCRETE STRUCTURES HOMEWORK FOR WEDNESDAY WEEK 3

Problem 1. Let $f:A\to B$ be a function. Show that a function $g:B\to A$ such that $f\circ g=\mathrm{id}_B$ exists if and only if f is surjective.

Problem 2. Suppose that f and g are composable functions.

- (a) If $g \circ f$ is surjective, does g have to be surjective? Does f have to be surjective?
- (b) If $g \circ f$ is injective, does g have to be injective? Does f have to be injective? (Explain all of your reasoning.)