MATH 113: DISCRETE STRUCTURES HOMEWORK DUE WEDNESDAY WEEK 12

Problem 1. Use the Euclidean algorithm to compute the following (showing your work):

(a) gcd(20, 45) (b) gcd(247, 299) (c) gcd(51, 897).

Problem 2. Use the Euclidean algorithm to compute the gcd of 198 and 168 and find integers m and n such that

gcd(198, 168) = 198m + 168n.

Show your work.

Problem 3.

- (a) Show that if *n* is positive integer of the form 4k + 3 for some integer *k*, then *n* is not a perfect square. (Hint: Suppose $n = m^2$. We can then write m = 4q + r for some $r \in \{0, 1, 2, 3\}$. Consider the remainders of the quantities $(4q)^2$, $(4q+1)^2$, $(4q+2)^2$, and $(4q+3)^2$ upon division by 4.)
- (b) Show that no integer in the sequence

$$11, 111, 1111, 11111, \ldots$$

is a perfect square. [Hint: Use the fact that $111 \dots 1111 = 111 \dots 1108 + 3$.]