MATH 113: DISCRETE STRUCTURES HOMEWORK DUE WEDNESDAY WEEK 6

Problem 1. A graph is *k*-regular if each of its vertices has degree *k*.

- (a) Draw a 3-regular graph on 6 vertices.
- (b) Prove that there are no 3-regular graphs on 5 vertices.

Problem 2. If *G* is a graph and *e* is an edge of *G*, define G - e to be the graph obtained from *G* by removal of *e* (but not the endpoints of *e*). Recall that to say a graph is *connected* means that every pair of its vertices can be connected by a path.

- (a) Give an example of a connected graph G with an edge e such that G e is not connected.
- (b) Suppose *G* is a connected graph and *e* is an edge of *G* that is part of a cycle. Prove that removal of *e* does not disconnect the graph. Your proof is required to start with the line: "Let *u* and *v* be vertices of *G*." It should then show there must be a path in G e connecting *u* and *v*.