

PROBLEM 1. In what sense is  $\sum_{n=0}^{\infty} i^n$  a sequence? Draw this sequence in the complex plane.

PROBLEM 2. Let  $\{a_n\}$  be a sequence of real numbers.

- (a) Critique the statement that  $\sum_{n=0}^{\infty} a_n$  is convergent if and only if its sequence of partial sums is bounded. Give a proof or a counterexample for both implications.
- (b) Does anything change if  $\{a_n\}$  is a sequence of *nonnegative* real numbers?

PROBLEM 3. Determine whether the following series converge, and in the case one does, find its sum. If the sum is complex, express the answer in the form  $a + bi$  with  $a, b \in \mathbb{R}$ .

$$(a) \sum_{n=2}^{\infty} (-1)^n \frac{3^{2n+2}}{10^n} \quad (b) \sum_{n=0}^{\infty} \left(\frac{2+i}{2}\right)^n \quad (c) \sum_{n=0}^{\infty} \left(\frac{3+i}{5}\right)^n.$$

PROBLEM 4. Express  $0.99999\dots$  as a geometric series, and sum the series. Do the same for  $6.232323\dots$  to express this number as a quotient of integers.

PROBLEM 5. Sum the series  $\sum_{n=1}^{\infty} \frac{1}{n(n+2)}$ .