

1. In many areas of application people are interested in the variability of data relative to the mean. The usual statistic for expressing this idea is the *coefficient of variation* or CV: the size of the standard deviation relative to the mean, or  $\sigma/\mu$ . You will often see the CV expressed as a percentage, that is if  $\sigma/\mu = .05$ , the CV may be expressed as 5%.

- (a) Generate 100 samples of size 25 from a Normal(10, 1) distribution and find the CV for each sample as follows:

```
set.seed(12345)
X <- matrix(rnorm(100*25,10),nrow=100)
m <- apply(X,1,mean)
s <- apply(X,1,sd)
CV <- s/m
```

Compute the mean and standard deviation of the set of 100 CV's. Note: here the true CV is 1/10.

- (b) Using the 'Delta Method', find an expression for the approximate standard error of the CV. Since know the distribution of both the sample mean  $\bar{x}$  and sample SD  $s^2$ , we can apply the method to

$$\frac{\sqrt{s^2}}{\bar{x}}.$$

- (c) Write an R function to evaluate your formula for the SE of the CV. It should take the raw dataset as input.
- (d) Apply that function to the samples generated above, that is

```
SE <- apply(X,1,yourfun)
```

How do the Delta Method SE's compare to the standard deviation of the 100 CV's computed in the first part?